

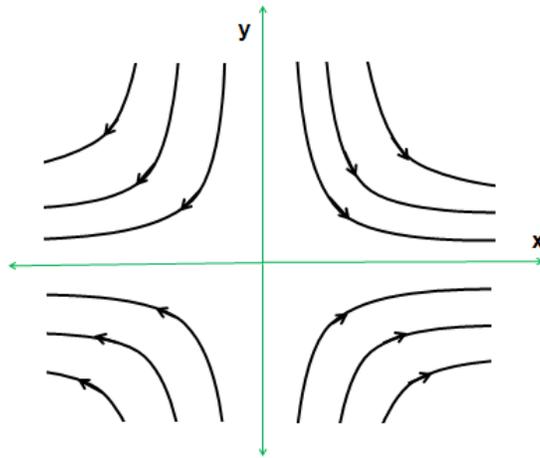
### Solution to Problem 115F:

On the planar, incompressible flow given by  $\psi = Axyt$ :

(a) Streamlines are lines of constant  $\psi$  at some specific time,  $t$ , and the equation for those lines is therefore

$$xy = \psi/At = \text{constant} \quad (1)$$

so the flow is as follows:



(b) The velocities of the flow are:

$$u(x, y, t) = \frac{\partial \psi}{\partial y} = Axt \quad (2)$$

$$v(x, y, t) = -\frac{\partial \psi}{\partial x} = -Ayt \quad (3)$$

(c) The pathlines of the flow: Since  $u = Axt = dx/dt$  along a pathline it follows by integration that

$$\ln x = At^2/2 + \text{constant} \quad (4)$$

and the constant is  $\ln x_0$  so that

$$x = x_0 \exp(At^2/2) \quad (5)$$

Similarly since  $v = -Ayt = dy/dt$  along the pathline

$$y = y_0 \exp(-At^2/2) \quad (6)$$